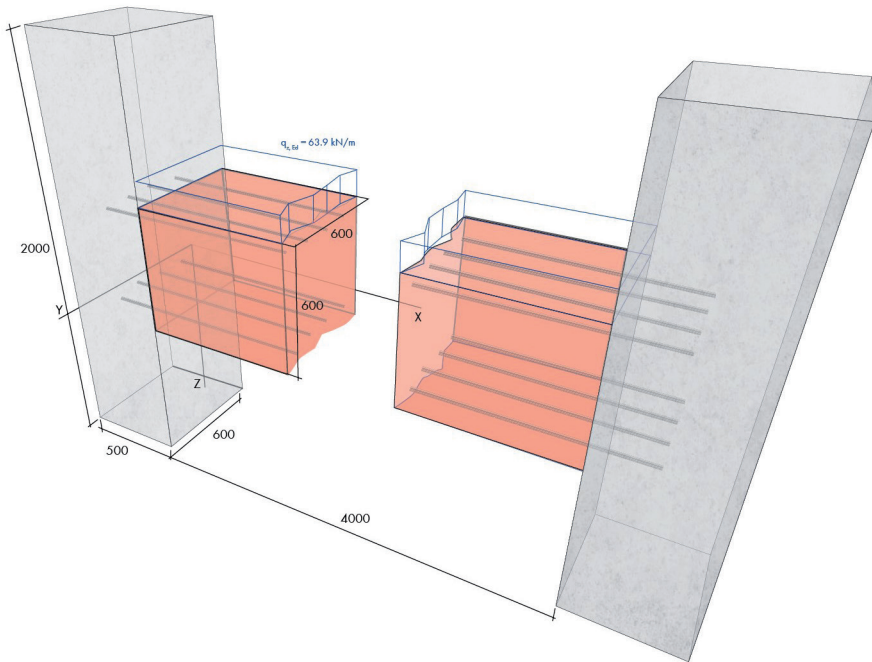


# DESIGN EXAMPLE - BEAM BETWEEN TWO COLUMNS



DESIGN EXAMPLES

Base material of existing & new			
Characteristic compressive cube strength of concrete at 28 days		$f_{ck,cube} =$	25 N/mm <sup>2</sup>
Characteristic compressive cube strength of concrete at 28 days		$f_{ck,cyl} =$	30 N/mm <sup>2</sup>
<b>Cracked concrete</b>	✓	<b>Non-cracked concrete</b>	
Roughness of joint		=	rough

Geometry			
<b>Existing structure:</b>			
Height		H =	2000 mm
Width		W =	600 mm
Depth		D =	500 mm
<b>New structure:</b>			
Height		H =	600 mm
Width		W =	600 mm
Span length		L =	4000 mm
Effective span length		$L_{ef} =$	4500 mm

<b>Reinforcement</b>			
Injection Anchor			WIT-UH 300
Top reinforcement diameter	$\varnothing =$	16	mm
Bottom reinforcement diameter	$\varnothing =$	16	mm
<b>Top reinforcement:</b>			
Number of bars	$n_{\text{Top}}$	4	
Anchorage length	$l_{\text{bd},1}$	193	mm
Drill hole depth	$l_{v1}$	250	mm
Drill diameter	$d_0$	20	mm
<b>Bottom reinforcement:</b>			
Number of bars	$n_{\text{Bot}}$	4	
Anchorage length	$l_{\text{bd},2}$	196	mm
Drill hole depth	$l_{v2}$	250	mm
Drill diameter	$d_0$	20	mm

<b>Actions</b>
Beam self-weight = $25 \cdot (0.6 \cdot 0.6) \cdot 1.35 = 12.15 \text{ kN/m}$
Slab self-weight = $25 \cdot 0.25 \cdot 4 \text{ m} \cdot 1.35 = 33.75 \text{ kN/m}$
=> Dead load = $12.15 + 33.75 = 45.9 \text{ kN/m}$
Imposed load = $3 \text{ kN/m}^2$ (Category B - Office)
=> Live load = $3 \cdot 4 \text{ m} \cdot 1.5 = 18 \text{ kN/m}$

<b>A - Determination of the additional normal force due to shear loading</b>		
$F_{\text{Ed}}$	=	$\max( V_{z,\text{ed}}  \cdot a/z; 0.5 \cdot  V_{z,\text{ed}} )$ EN 1992-1-1: 9.2.1.4 (9.3); NCI 9.3DE
$V_{z,\text{ed}}$	=	143.775 kN
$F_{\text{Ed}}$	=	159.75 kN

<b>B - Verification of steel</b>		
<b>Bottom reinforcement (new)</b>		
$\beta_{\text{sb},2}$	=	$\sigma_{\text{Ed}} / \sigma_{\text{Rd}}$ degree of capacity utilisation
$\sigma_{\text{Ed}}$	=	$N_{\text{Ed}}/A = 159.74 / 4 (\pi \times 16^2/4) = 198.63 \text{ N/mm}^2$ Design value of the actions
$\sigma_{\text{R}}$	=	$f_{yk} / \gamma_{\text{Ms}} = 500 / 1.15 = 434.78 \text{ N/mm}^2$
$\beta_{\text{sb},2}$	=	$\sigma_{\text{Ed}} / \sigma_{\text{Rd}} = 198.63 / 434.78 = 0.46$ degree of capacity utilisation

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<b>C - Verification of concrete</b>			
<b>Bottom reinforcement (anchorage)</b>			
$l_{bd}$	=	$\max(\alpha_1 \cdot \alpha_2 \cdot \alpha_3 \cdot \alpha_5 \cdot l_{b,rd}; l_{b,min})$	EN 1992-1-1: 8.4.4 (8.4)
$l_{b,rd}$	=	$(d/4) \cdot (\sigma_{sd} / f_{bd}) = (16/4) \times (198.63 / 2.7)$ = 294 mm	EN 1992-1-1: 8.4.3 (8.3)
$l_{b,min}$	=	$\max(0.3 \cdot \alpha_1 \cdot \alpha_4 \cdot l_{b,rd,min}; 2/3 \cdot 10 \cdot d;$ $2/3 \cdot 100 \text{ mm}) \cdot 1.0$	EN 1992-1-1: 8.4.4 (8.6)
$l_{b,rd,min}$	=	$(d/4) \cdot (f_{yd} / f_{bd}) = (16/4) \times (500/1.15/2.7)$ = 644 mm	EN 1992-1-1: 8.4.3 (8.3)
$l_{b,min}$	=	$\max(0,3 \times 1 \times 1 \times 644 ; 2/3 \times 10 \times 16; 2/3$ $\times 100) = 193.2 \text{ mm}$	
$l_{bd}$	=	$\max(1 \times 1 \times 1 \times 0.67 \times 294 ; 193.2) =$ 196.9 mm	
$l_v$	=	<span style="color: red; font-weight: bold;">250</span> mm	9.2.1.4 (3) extension to the calculated support position (effective span), which is in this case in the middle of the column (Commentary of the German National Annex)

<b>Shear at the joint</b>			
$\beta_{joint}$	=	$V_{Edi} / V_{Rdi}$	degree of capacity utilisation
$V_{Edi}$	=	$\beta \cdot V_{Ed} / (z \cdot b_i) = 1 \times 143.775 / (600 \times 600)$ = 0.399 N/mm <sup>2</sup>	EN 1992-1-1: 6.2.5 (6.24)
$V_{Rdi}$	=	$M_{in} (V_{Rdic}; V_{Rc,max})$	EN 1992-1-1: 6.2.5 (1)
$V_{Rdic}$	=	$c \cdot f_{ctd} + (\mu \cdot \sigma_D + \mu \cdot \sigma_z) = 0.4 \times 1.0174 +$ $(0.7 \times 0 + 0.7 \times 0) = 0.407 \text{ N/mm}^2$	EN 1992-1-1: 6.2.5 (6.25)
$V_{Rc,max}$	=	$0.5 \cdot v \cdot f_{cd}$	EN 1992-1-1: 6.2.5 (6.25)
$f_{cd}$	=	$\alpha_{cc} \cdot f_{ck} / \gamma_c = 0.85 \times 20 / 1.5 = 14.17 \text{ N/mm}^2$	EN 1992-1-1: 3.1.6 (3.15)
$V_{Rc,max}$	=	$0.5 \cdot v \cdot f_{cd} = 0.5 \times 0.5 \times 14.17$ = 3.54 N/mm <sup>2</sup>	EN 1992-1-1: 6.2.5 (6.25)
$\beta_{joint}$	=	$V_{Edi} / V_{rdi} = 0.399 / 0.407 = 0.98$	Degree of capacity utilisation

